

# Package: easyCODA (via r-universe)

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**Author** Michael Greenacre [aut, cre]

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**Description** Univariate and multivariate methods for compositional data analysis, based on logratios. The package implements the approach in the book Compositional Data Analysis in Practice by Michael Greenacre (2018), where accent is given to simple pairwise logratios. Selection can be made of logratios that account for a maximum percentage of logratio variance. Various multivariate analyses of logratios are included in the package.

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## Contents

easyCODA-package . . . . .	2
ACLUST . . . . .	4
ALR . . . . .	6
BAR . . . . .	7
CA . . . . .	9
CIplot_biv . . . . .	10
CLOSE . . . . .	12
CLR . . . . .	13
cups . . . . .	14
DOT . . . . .	14
DUMMY . . . . .	16
FINDALR . . . . .	16
fish . . . . .	18
ILR . . . . .	18
invALR . . . . .	19
invCLR . . . . .	20
invSLR . . . . .	21
LR . . . . .	22
LR.VAR . . . . .	23
LRA . . . . .	25
PCA . . . . .	27
PLOT.CA . . . . .	29
PLOT.LRA . . . . .	30
PLOT.PCA . . . . .	31
PLOT.RDA . . . . .	33
PLR . . . . .	34
RDA . . . . .	35
SLR . . . . .	37
STEP . . . . .	39
STEPR . . . . .	41
time . . . . .	44
VAR . . . . .	45
veg . . . . .	46
WARD . . . . .	46
<b>Index</b>	<b>49</b>

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easyCODA-package

*Compositional Data Analysis in Practice*

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### Description

Univariate and multivariate methods for compositional data analysis, based on logratios. The package implements the approach in the book *Compositional Data Analysis in Practice* by Michael Greenacre (2018), where accent is given to simple pairwise logratios. Selection can be made of logratios that account for a maximum percentage of logratio variance. Various multivariate analyses of logratios are included in the package.

**Details**

The DESCRIPTION file:

```

Package:          easyCODA
Type:             Package
Version:          0.40.2
Date:             2024-08-25
Title:            Compositional Data Analysis in Practice
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Maintainer:       Michael Greenacre <michael.greenacre@upf.edu>
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```

Index of help topics:

```

ACLUST           Amalgamation clustering of the parts of a
                  compositional data matrix
ALR              Additive logratios
BAR              Compositional bar plot
CA              Correspondence analysis
CIplot_biv       Bivariate confidence and data ellipses
CLOSE           Closure of rows of compositional data matrix
CLR             Centred logratios
DOT             Dot plot
DUMMY           Dummy variable (indicator) coding
FINDALR         Find the best ALR transformation
ILR            Isometric logratio
LR             All pairwise logratios
LR.VAR         Total logratio variance
LRA            Logratio analysis
PCA            Principal component analysis
PLOT.CA        Plot the results of a correspondence analysis
PLOT.LRA       Plot the results of a logratio analysis
PLOT.PCA       Plot the results of a principal component
                  analysis
PLOT.RDA       Plot the results of a redundancy analysis
PLR           Pivot logratios

```

RDA	Redundancy analysis
SLR	Amalgamation (summed) logratio
STEP	Stepwise selection of logratios
STEPR	Stepwise selection of pairwise logratios for generalized linear modelling
VAR	Variance of a vector of observations, dividing by n rather than n-1
WARD	Ward clustering of a compositional data matrix
cups	Dataset: RomanCups
easyCODA-package	Compositional Data Analysis in Practice
fish	Dataset: FishMorphology
invALR	Inverse of additive logratios
invCLR	Inverse of centred logratios
invSLR	Inverse of full set of amalgamation balances
time	Dataset: TimeBudget
veg	Dataset: Vegetables

**Author(s)**

Michael Greenacre [aut, cre]

Maintainer: Michael Greenacre <michael.greenacre@upf.edu>

**References**

Greenacre, Michael (2018) Compositional Data Analysis in Practice. Chapman & Hall / CRC Press

**See Also**

[ca](#)

**Examples**

```
# Roman cups glass compositions
data("cups")
# unweighted logratio analysis
cups.ulra <- LRA(cups, weight=FALSE)
PLOT.LRA(cups.ulra)
# weighted logratio analysis
cups.wlra <- LRA(cups)
PLOT.LRA(cups.wlra)
```

---

ACLUST

*Amalgamation clustering of the parts of a compositional data matrix*

---

**Description**

This function clusters the parts of a compositional data matrix, using amalgamation of the parts at each step.

**Usage**

```
ACLUST(data, weight = TRUE, close = TRUE)
```

**Arguments**

data	Compositional data matrix, with the parts as columns
weight	TRUE (default) for weighting using part averages of closed compositions, FALSE for unweighted analysis, or a vector of user-defined column weights
close	TRUE (default) will close the rows of data prior to clustering, FALSE leaves data as it is

**Details**

The function ACLUST performs amalgamation hierarchical clustering on the parts (columns) of a given compositional data matrix, as proposed by Greenacre (2019). At each step of the clustering two clusters are amalgamated that give the least loss of explained logratio variance.

**Value**

An object which describes the tree produced by the clustering process on the  $n$  objects. The object is a list with components:

merge	an $n-1$ by 2 matrix. Row $i$ of merge describes the merging of clusters at step $i$ of the clustering. If an element $j$ in the row is negative, then observation $-j$ was merged at this stage. If $j$ is positive then the merge was with the cluster formed at the (earlier) stage $j$ of the algorithm. Thus negative entries in merge indicate agglomerations of singletons, and positive entries indicate agglomerations of non-singletons.
height	a set of $n-1$ real values (non-decreasing for ultrametric trees). The clustering height: that is, the value of the criterion associated with the clustering method for the particular agglomeration.
order	a vector giving the permutation of the original observations suitable for plotting, in the sense that a cluster plot using this ordering and matrix merge will not have crossings of the branches
labels	a vector of column labels, the column names of data

**Author(s)**

Michael Greenacre

**References**

Greenacre, M. (2018), *Compositional Data Analysis in Practice*, Chapman & Hall / CRC.  
Greenacre, M. (2019), Amalgamations are valid in compositional data analysis, can be used in agglomerative clustering, and their logratios have an inverse transformation. *Applied Computing and Geosciences*, open access.

**See Also**

[hclust](#), [WARD,CLR](#), [LR.VAR](#), [CLOSE](#)

**Examples**

```
data(cups)

# amalgamation clustering (weighted parts)
cups.aclust <- ACLUS(cups)
plot(cups.aclust)

# reproducing Figure 2(b) of Greenacre (2019) (unweighted parts))
# dataset Aar is in the compositions package
# aar is a subset of Aar
# code given here within the 'dontrun' environment since external package 'compositions' required
## Not run:
  library(compositions)
  data(Aar)
  aar <- Aar[,c(3:12)]
  aar.aclust <- ACLUS(aar, weight=FALSE)
# the maximum height is the total variance
# convert to percents of variance NOT explained
  aar.aclust$height <- 100 * aar.aclust$height / max(aar.aclust$height)
  plot(aar.aclust, main="Parts of Unexplained Variance", ylab="Variance (percent)")

## End(Not run)
```

---

 ALR

*Additive logratios*


---

**Description**

Computation of additive logratios (ALRs) with respect to a specified part.

**Usage**

```
ALR(data, denom=ncol(data), weight=TRUE, stats=FALSE)
```

**Arguments**

<code>data</code>	A compositional data frame or matrix
<code>denom</code>	Number of part used in the denominator
<code>weight</code>	Logical indicating if varying weights are returned(default:TRUE). If FALSE, un-weighted (equal) weights are returned. Alternatively a set of positive weights can be specified.
<code>stats</code>	Logical indicating if means, variances and total variance of the ALRs are returned (default:FALSE)

**Details**

The function ALR computes a set of additive logratios (ALRs) with respect to a specified part (by default, the last part).

**Value**

LR	The additive logratios (ALRs)
LR.wt	The weights assigned to the ALRs
denom	The index of the denominator used in the computation of the ALRs
part.names	The part names in the data, i.e. column names
part.wt	The part weights
means	The means of the ALRs (only returned if stats = TRUE)
vars	The variances of the ALRs (only returned if stats = TRUE)
totvar	The total variance of the ALRs (only returned if stats = TRUE)

**Author(s)**

Michael Greenacre

**References**

Aitchison, J. (1986), *The Statistical Analysis of Compositional Data*, Chapman & Hall.  
 Greenacre, M. (2018), *Compositional Data Analysis in Practice*, Chapman & Hall / CRC Press.

**See Also**

[invALR](#), [LR](#), [CLR](#), [invCLR](#), [LR.VAR](#)

**Examples**

```
data(veg)
ALR(veg, denom=2)
```

---

 BAR

*Compositional bar plot*


---

**Description**

Horizontal bar plot of compositional data

**Usage**

```
BAR(data, cols=rainbow(ncol(data)), col.names=colnames(data),
     row.names=rownames(data), order.column=NA, eps=0.5, main="", ylab="",
     ylim=c(0,nrow(data)), xlim=c(0,100), cex=1, truncate=NA)
```

**Arguments**

<code>data</code>	Compositional data matrix or data frame with compositions in rows, parts in columns
<code>cols</code>	Colours of points for each part, default rainbow
<code>col.names</code>	Part names, if modified
<code>row.names</code>	Sample names, if modified
<code>order.column</code>	By default parts are taken in order of columns, but can be re-ordered using this option
<code>eps</code>	Small space between bars, can be modified
<code>main</code>	Heading
<code>ylab</code>	Vertical axis label
<code>ylim</code>	Vertical axis limits (default is the number of rows in data)
<code>xlim</code>	Horizontal axis limits (default <code>c(0,100)</code> )
<code>cex</code>	Character size scaling factor for labels
<code>truncate</code>	Truncate part (column) names to this number of characters for legend

**Details**

The function `BAR` makes a BAR plot for specified groups of points, which can be in columns of a matrix or data frame.

**Author(s)**

Michael Greenacre

**References**

Greenacre, M. (2016), Data reporting and visualization in ecology, *Polar Biology*: 39, 2189-2205.

**See Also**

[DOT](#)

**Examples**

```
# Vegetables data set: order samples by carbohydrates
data(veg)
BAR(veg, order.column=2)
data(time)
# TimeBudget data set: put domestic work in first column and order by it
BAR(time[,c(2,1,3,4,5,6)], order.column=1, main="Time Budget")
```



**Description**

Computation of correspondence analysis on a table of nonnegative data.

**Usage**

```
CA(data, nd = 2, suprow = NA, supcol = NA)
```

**Arguments**

data	A data frame or matrix of nonnegative data (no negative values)
nd	Number of dimensions for summary solution if not 2 (default)
suprow	Indices of rows that are supplementary points
supcol	Indices of columns that are supplementary points

**Details**

The function `CA` is a simple wrapper for the `ca` function in the **ca** package (Nenadic and Greenacre, 2007), for compatibility within the **easyCODA** package.

Supplementary rows and columns can be declared (also known as passive points) – these do not contribute to the solution but are positioned on the solution axes.

The function borrows the structure and functions of the `ca` package, which is required, and produces a `ca` object, and the same `print`, `summary` and `plot` methods can be used, as for a `ca` object. It additionally exports the principal coordinates of both the rows and columns, not presently found in the `ca` package.

**Value**

sv	Singular values
nd	Number of dimensions in solution results
rownames	Row names
rowmass	Row weights
rowdist	Row logratio distances to centroid
rowinertia	Row inertias
rowcoord	Row standard coordinates
rowpcoord	Row principal coordinates
rowsup	Indices of row supplementary points
colnames	Column names
colmass	Column weights

coldist	Column logratio distances to centroid
colinertia	Column inertias
colcoord	Column standard coordinates
colpcoord	Column principal coordinates
N	The compositional data table

### Author(s)

Michael Greenacre

### References

Nenadic, O. and Greenacre, M. (2007). Correspondence analysis in R, with two- and three-dimensional graphics: The ca package. *Journal of Statistical Software*, **20 (3)**, <https://www.jstatsoft.org/v20/i03/>

### See Also

[PLOT.CA](#), [plot.ca](#), [summary.ca](#), [print.ca](#)

### Examples

```
# CA of the Roman cups data (symmetric map)
data("cups")
PLOT.CA(CA(cups))
```

---

CIplot\_biv

*Bivariate confidence and data ellipses*

---

### Description

Draws confidence and data ellipses in bivariate scatterplots

### Usage

```
CIplot_biv(x, y, group, wt=rep(1/length(x),length(x)),
           varnames=c("x","y"), groupnames=sort(unique(group)),
           groupcols=rainbow(length(unique(group))),
           shownames=TRUE, xlim=c(NA,NA), ylim=c(NA,NA),
           lty=1, lwd=1, add=FALSE, alpha=0.95, ellipse=0,
           shade=FALSE, alpha.f=0.2, frac=0.01, cex=1)
```

**Arguments**

x	x-variable (horizontal) of scatterplot
y	y-variable (vertical) of scatterplot
group	Grouping variable
wt	Set of weights on the cases (operates when ellipse=1)
varnames	Vector of two labels for the axes (default is x and y)
groupnames	Vector of labels for the groups (default is 1, 2, etc...)
groupcols	Vector of colours for the groups
shownames	Whether to show group names at group centroids or not (default is TRUE)
xlim	Possible new x-limits for plot
ylim	Possible new y-limits for plot
lty	Line type for the ellipses (default is 1)
lwd	Line width for the ellipses (default is 1)
add	=TRUE if ellipses/intervals are added to existing plot (default is FALSE)
alpha	Confidence level of ellipses (default is 0.95)
ellipse	Type of ellipse (see Details below; default is 0 for normal-based ellipses)
shade	=TRUE for ellipse shading (default=FALSE)
alpha.f	Shading fraction (default is 0.2)
frac	Proportional part defining the width of the bars at the edges of confidence intervals (for ellipse=3 and 4)
cex	Character expansion factor for group names

**Details**

The function `CIplot_biv` makes various types of confidence and data ellipses, according to option `ellipse`. Set `ellipse<0` for regular data-covering ellipses. Set `ellipse=0` (default) for normal-theory confidence ellipses. Set `ellipse=1` for bootstrap confidence ellipses. The option `ellipse=2` for the delta method is not implemented yet. Set `ellipse=3` for normal-theory confidence error bars lined up with axes. Set `ellipse=4` for bootstrap confidence error bars along axes. The package `ellipse` is required.

**Author(s)**

Michael Greenacre

**References**

Greenacre, M. (2016), Data reporting and visualization in ecology, *Polar Biology*, 39:2189-2205.

**See Also**

[DOT](#)

**Examples**

```
# Generate some bivariate normal data in three groups with different means
# Means (1,0), (0,1) and (0,0)
means <- matrix(c(1,0,0,1,0,0), ncol=3)
data <- matrix(nrow=300, ncol=2)
groups <- sample(rep(c(1,2,3), 100))
for(i in 1:300) data[i,] <- rnorm(c(1,1), mean=means[,groups[i]])
# Plot confidence ellipses with shading
CIplot_biv(data[,1], data[,2], group=groups, shade=TRUE)
```

CLOSE

*Closure of rows of compositional data matrix***Description**

This function closes (or normalizes) the rows of a compositional data matrix, resulting in rows summing to 1.

**Usage**

```
CLOSE(x)
```

**Arguments**

x                      Compositional data matrix.

**Details**

Compositional data carry relative information. It is sometimes required to close the data so that each row of observations sums to 1. The function CLOSE performs the closure.

**Value**

The closed compositional data matrix.

**Author(s)**

Michael Greenacre

**References**

Greenacre, M. (2018), *Compositional Data Analysis in Practice*, Chapman & Hall / CRC.

**Examples**

```
data(cups)
apply(cups, 2, sum)
cups <- CLOSE(cups)
apply(cups, 2, sum)
```

---

CLR	<i>Centred logratios</i>
-----	--------------------------

---

**Description**

Computation of centred logratios (CLRs).

**Usage**

```
CLR(data, weight=TRUE)
```

**Arguments**

data	A compositional data frame or matrix
weight	Logical indicating if varying weights are returned(default:TRUE). If FALSE, un-weighted (equal) weights are returned. Alternatively a set of positive weights can be specified.

**Details**

The function CLR computes the set of centred logratios (CLRs).

**Value**

LR	The centred logratios (CLRs)
LR.wt	The weights assigned to the CLRs

**Author(s)**

Michael Greenacre

**References**

Aitchison, J. (1986), *The Statistical Analysis of Compositional Data*, Chapman & Hall.  
Greenacre, M. (2018), *Compositional Data Analysis in Practice*, Chapman & Hall / CRC Press.

**See Also**

[invCLR](#), [ALR](#), [invALR](#), [LR](#), [LR.VAR](#)

**Examples**

```
data(veg)  
CLR(veg)
```

cups

*Dataset: RomanCups***Description**

This data set consists of the compositions of 11 oxides in 47 Roman cups found at an archaeological site in eastern England. Compositions are expressed as percentages.

**Usage**

```
data(cups)
```

**Format**

Data frame containing the 47 x 11 matrix.

**Source**

Baxter MJ, Beardah CC, Cool HEM and Jackson CM (2005) Compositional data analysis of some alkaline glasses. *Mathematical Geology* 37: 183-196.

DOT

*Dot plot***Description**

Simple dot plot of original data

**Usage**

```
DOT(data, cols=NA, names=NA, groups=NA, pch=NA, horizon=FALSE, jitter=1,
     xscale=NA, xscalefac=1, yaxis=TRUE, shownames=TRUE, main="", ylab="",
     xlim=c(NA,NA), ylim=c(NA, NA), cex=1)
```

**Arguments**

data	Matrix or data frame with data groups in columns; alternatively, a single vector but then groups (if any) have to specified with the groups option
cols	Colours of points for each sample, default rainbow
names	Labels for variables, by default the column names of data, or group names
groups	Group codes to split the data vector into separate plots
pch	Point character
horizon	TRUE if horizontal gray dashed lines required at "nice" y-values (default FALSE, not implemented yet)

jitter	1 by default, increase or decrease slightly for more jitter
xscale	User-supplied positions of points on horizontal axis
xscalefac	1 by default, rescale the positions on horizontal axis
yaxis	TRUE by default, FALSE to suppress and optionally add afterwards
shownames	TRUE by default; FALSE to not show group names and add them externally
main	Heading
ylab	Vertical axis label
xlim	Horizontal axis limits
ylim	Vertical axis limits
cex	Character size adjustment for labels

### Details

The function DOT makes a dot plot for specified groups of points, which can be in columns of a matrix or data frame, or in a single vector with group codes specified separately.

### Author(s)

Michael Greenacre

### References

Greenacre, M. (2016), Data reporting and visualization in ecology, *Polar Biology*, 39:2189-2205.

### See Also

[BAR](#)

### Examples

```
# Dot plot of columns of Vegetables data set
data(veg)
DOT(veg)
# Dot plot of domestic work column of TimeBudget data set, split by sex
data(time)
DOT(time[,2], groups=substr(rownames(time),3,3), cols=c("blue","red"), ylim=c(0,20),
  jitter=2, main="Percentage of Domestic Work")
```

DUMMY

*Dummy variable (indicator) coding*

---

**Description**

Convert categorical variable to dummy (0/1) coding

**Usage**

```
DUMMY(x, catnames=NA)
```

**Arguments**

x	Variable (vector) of categorical data to be coded
catnames	Category names

**Details**

The function DUMMY takes a categorical variable and converts it to a set of dummy variables (zeros and ones), where the ones indicate the corresponding category. There are as many columns in the result as there are unique categories in the input vector.

**Author(s)**

Michael Greenacre

**Examples**

```
# Indicator (dummy) coding of sex in FishMorphology data set
data(fish)
sex <- fish[,1]
sex.Z <- DUMMY(sex, catnames=c("F", "M"))
```

---

FINDALR*Find the best ALR transformation*

---

**Description**

Searching over every possible reference part for choosing an optimal ALR transformation.

**Usage**

```
FINDALR(data, weight=FALSE)
```



**Arguments**

data	Compositional data matrix, with the parts as columns
weight	FALSE (default) for equally weighted parts, TRUE when weights are in data list object, or a vector of user-defined part weights

**Details**

The function FINDALR considers every possible set of additive logratio (ALR) transformations, by trying each of the references. For each set the closeness to isometry is measured by the Procrustes correlation. In addition, the variance of the log-transformed reference is also computed. The reference with highest Procrustes correlation and the reference with the lowest variance of its log-transform are identified. The number of ALRs computed is equal to 1 less than the number of rows or columns, whichever is the smallest.

**Value**

An object which describes the tree produced by the clustering process on the n objects. The object is a list with components:

totvar	Total logratio variance
procrust.cor	The Procrustes correlations of the ALRs using each reference
procrust.max	The value of the highest Procrustes correlation
procrust.ref	The reference corresponding to the highest correlation
var.log	Variances of the log-transformed references
var.min	The value of the lowest variance
var.ref	The reference corresponding to the lowest variance

**Author(s)**

Michael Greenacre

**References**

- Greenacre, M., Martinez-Alvaro, M. and Blasco, A. (2021), Compositional data analysis of microbiome and any-omics datasets: a validation of the additive logratio transformation, *Frontiers in Microbiology* 12: 2625
- Gower, J. and Dijksterhuis, G.B. (2004), *Procrustes Problems*. Oxford University Press
- Greenacre, M. (2018), *Compositional Data Analysis in Practice*, Chapman & Hall / CRC

**See Also**

[ALR](#)

**Examples**

```
# For the fish morphometric data, first close (normalize)
# then loop over the 26 possible references
data(fish)
FINDALR(CLOSE(fish[,4:29]))
# Note that for the default option weight=FALSE closing the data is not necessary
```

---

fish	<i>Dataset: FishMorphology</i>
------	--------------------------------

---

**Description**

This data set consists of the sex, habitat, mass and then 26 morphometric measurements on 75 fish (Arctic charr)

**Usage**

```
data(fish)
```

**Format**

Data frame containing the 75 x 29 matrix. Column 1 contains sex (1=female, 2=male). Column 2 contains habitat (1=litoral, 2=pelagic). Column 3 contains the mass in grams. Columns 4 to 29 contain the 26 morphometric measurements.

**Source**

Greenacre, M and Primicerio, R (2010) Multivariate Analysis of Ecological Data. BBVA Foundation, Bilbao. Free download at [www.multivariatestatistics.org](http://www.multivariatestatistics.org)

---

ILR	<i>Isometric logratio</i>
-----	---------------------------

---

**Description**

Computation of a single isometric logratio (ILR)

**Usage**

```
ILR(data, numer=NA, denom=NA, weight=TRUE)
```

**Arguments**

data	A compositional data frame or matrix
numer	Vector of parts in the numerator
denom	Vector of parts in the denominator
weight	Logical indicating if a varying weight is returned (default:TRUE). If FALSE, a weight based on equally-weighted parts is returned. Alternatively a positive weight can be specified.

**Details**

The function ILR computes a single isometric logratio based on the specified numerator and denominator parts that define the two geometric means in the ratio.

**Value**

LR	The isometric logratio (ILR)
LR.wt	The weight assigned to the ILR

**Author(s)**

Michael Greenacre

**References**

Aitchison, J. (1986), *The Statistical Analysis of Compositional Data*, Chapman & Hall.  
 Greenacre, M. (2018), *Compositional Data Analysis in Practice*, Chapman & Hall / CRC Press.

**See Also**

[SLR](#), [ALR](#), [PLR](#), [LR](#)

**Examples**

```
data(veg)
ILR(veg, numer=1, denom=2:3)
```

---

 invALR

*Inverse of additive logratios*

---

**Description**

Given additive logratios (ALRs) with respect to a specified part, compute the inverse (i.e. original parts)

**Usage**

```
invALR(ALRmatrix, part.names=paste("part", 1:(ncol(ALRmatrix)+1), sep=""), denom=NA)
```

**Arguments**

ALRmatrix	A matrix of additive logratios (ALRs) with respect to a specified part)
part.names	Part names in the reconstructed compositional data matrix
denom	The index of the denominator used in the computation of the ALRs (default: last part))

**Details**

The function `invALR` computes the original parts, given the additive logratios (ALRs)

**Value**

parts	The reconstructed parts (they add up to 1)
-------	--

**Author(s)**

Michael Greenacre

**References**

Aitchison, J. (1986), *The Statistical Analysis of Compositional Data*, Chapman & Hall.  
 Greenacre, M. (2018), *Compositional Data Analysis in Practice*, Chapman & Hall / CRC Press.

**See Also**

[ALR](#), [LR](#), [CLR](#), [invCLR](#), [LR.VAR](#)

**Examples**

```
data(veg)
# compute additive logratios with respect to second part
veg.ALR <- ALR(veg, denom=2)$LR
# recover original parts (to get same order, specify the denominator used originally)
invALR(veg.ALR, denom=2)
```

---

invCLR

*Inverse of centred logratios*

---

**Description**

Given centred logratios (CLRs), compute the inverse (i.e. recover the original parts)

**Usage**

```
invCLR(CLRmatrix, part.names=colnames(CLRmatrix))
```

**Arguments**

CLRmatrix      A matrix of centred logratios  
part.names      Part names in the reconstructed compositional data matrix

**Details**

The function `invCLR` computes the original parts, given the centred logratios (CLRs)

**Value**

parts            The reconstructed parts (they add up to 1)

**Author(s)**

Michael Greenacre

**References**

Aitchison, J. (1986), *The Statistical Analysis of Compositional Data*, Chapman & Hall.  
Greenacre, M. (2018), *Compositional Data Analysis in Practice*, Chapman & Hall / CRC Press.

**See Also**

[CLR](#), [ALR](#), [invALR](#), [LR.VAR](#)

**Examples**

```
data(veg)
# compute centred logratios
veg.CLR <- CLR(veg)$LR
# invert back to original parts (parts closed to sum to 1)
invALR(veg.CLR)
```

---

invSLR                      *Inverse of full set of amalgamation balances*

---

**Description**

Given a full set of amalgamation (or summation) balances (SLRs), compute the inverse (i.e. recover the original parts)

**Usage**

```
invSLR(SLRmatrix, part.names=NA, ratio.names=colnames(SLRmatrix))
```

**Arguments**

SLRmatrix	A matrix of amalgamation logratios, one less column than the number of parts
part.names	Part names in the reconstructed compositional data matrix
ratio.names	Definition of the amalgamation logratios

**Details**

The function `invSLR` computes the original parts, given the amalgamation logratios (CLRs). The amalgamation logratios are specified in `ratio.names` in the format `num/den` where `num` and `den` are the numerator and denominator amalgamations respectively. An amalgamation is specified as "`p1&p2&...`", where `p1`, `p2`, etc. are the parts summed in the amalgamation. For example, an SLR of the ratio `MnO/(CaO+P2O5)` would be names as "`MnO/CaO&P2O5`".

**Value**

<code>parts</code>	The reconstructed parts (they add up to 1)
--------------------	--

**Author(s)**

Michael Greenacre

**References**

Aitchison, J. (1986), *The Statistical Analysis of Compositional Data*, Chapman & Hall.  
 Greenacre, M. (2018), *Compositional Data Analysis in Practice*, Chapman & Hall / CRC Press.

**See Also**

[CLR](#), [ALR](#), [invALR](#), [LR.VAR](#)

**Examples**

```
data(veg)
# compute centred logratios
veg.CLR <- CLR(veg)$LR
# invert back to original parts (parts closed to sum to 1)
invALR(veg.CLR)
```

---

 LR

---

*All pairwise logratios*


---

**Description**

Computation of all pairwise logratios.

**Usage**

```
LR(data, ordering=1:ncol(data), weight=TRUE)
```

**Arguments**

data	A compositional data frame or matrix
ordering	A permutation of the columns (default: the original ordering)
weight	Logical indicating if varying weights are returned (default:TRUE). If FALSE, un-weighted (equal) weights are returned. Alternatively a set of positive weights can be specified.

**Details**

The function LR computes the complete set of pairwise logratios, in the order [1,2], [1,3], [2,3], [1,4], [2,4], [3,4], etc.

**Value**

LR	The pairwise logratios as columns of a data matrix
LR.wt	The weights assigned to the respective logratios

**Author(s)**

Michael Greenacre

**References**

Aitchison, J. (1986), *The Statistical Analysis of Compositional Data*, Chapman & Hall.  
 Greenacre, M. (2018), *Compositional Data Analysis in Practice*, Chapman & Hall / CRC Press.

**See Also**

[ALR](#), [invALR](#), [CLR](#), [invCLR](#), [LR.VAR](#)

**Examples**

```
data(veg)
LR(veg)
```

---

LR.VAR	<i>Total logratio variance</i>
--------	--------------------------------

---

**Description**

Computation of total (weighted)logratio variance.

**Usage**

```
LR.VAR(LRdata, row.wt = NA, weight=TRUE, vars=FALSE)
```

**Arguments**

LRdata	Matrix of logratios, either a vector or preferably the logratio object resulting from one of the functions ALR, CLR, PLR or LR
row.wt	Optional set of row weights (default: equal weights)
weight	Logical indicating if varying weights are returned(default:TRUE). If FALSE, unweighted (equal) weights are returned. Alternatively a set of positive weights can be specified.
vars	If TRUE, output individual variances as well (default FALSE)

**Details**

The function LR.VAR computes the sum of the logratio variances provided as input, using the weights in the logratio data object.

**Value**

LRtotvar	The total logratio variance
LRvars	(optional, if vars=TRUE, the individual logratio variances composing the total)

**Author(s)**

Michael Greenacre

**References**

Aitchison, J. (1986), *The Statistical Analysis of Compositional Data*, Chapman & Hall.  
Greenacre, M. (2018), *Compositional Data Analysis in Practice*, Chapman & Hall / CRC Press.

**See Also**

[LR](#), [ALR](#), [invALR](#), [CLR](#), [invCLR](#)

**Examples**

```
data(cups)
# These give identical total logratio variances (weighted, by default)
LR.VAR(CLR(cups))
LR.VAR(LR(cups))
# Summing over all sets of ALRs gives twice the variance
totvar <- 0
for(j in 1:ncol(cups)) totvar <- totvar + LR.VAR(ALR(cups, denom=j))
totvar/2
```



---

LRA *Logratio analysis*

---

### Description

Computation of weighted or unweighted logratio analysis of a samples-by-parts compositional data table.

### Usage

```
LRA(data, nd = 2, weight = TRUE, suprow = NA, row.wt = NA, amalg = NA, supamalg = FALSE)
```

### Arguments

<code>data</code>	A data frame or matrix of compositional data, with no zero values
<code>nd</code>	Number of dimensions for summary solution if not 2 (default)
<code>weight</code>	TRUE (default) for part weighting, FALSE for unweighted analysis, or a vector of user-defined part weights
<code>suprow</code>	Indices of rows that are supplementary points
<code>row.wt</code>	Optional user-defined set of positive weights for the rows (samples) (default: equal weights)
<code>amalg</code>	Optional list of amalgamated parts
<code>supamalg</code>	FALSE (default) when amalgamations are active and their subparts supplementary, TRUE when amalgamations are supplementary and their parts active

### Details

The function LRA computes a log-ratio analysis of a table of compositional data based on the singular value decomposition. By default the weighted log-ratio analysis is computed (Greenacre & Lewi 2009). For the unweighted logratio analysis (Aitchison & Greenacre 2002), specify the option `weight=FALSE`.

User-specified weights can be supplied, for the rows and/or the columns. Usually row weights are not specified, and are equal unless intentional weighting of the samples is desired. Default column weights (if `weight = TRUE`) are the part means of the true compositional table, thus summing to 1. User-specified part weights can be provided using the same `weight` option.

Supplementary rows can be declared (also known as passive points) – these do not contribute to the solution but are positioned on the solution axes.

Amalgamations can be defined and can either replace their constituent parts (default) or be declared supplementary using the `supamalg` option: `supamalg = FALSE` (default), `= TRUE` if all declared amalgamations are supplementary.

The function borrows the structure and functions of the `ca` package, which is required, and produces a `ca` object, and the same `print`, `summary` and `plot` methods can be used, as for a `ca` object.

**Value**

sv	Singular values
nd	Number of dimensions in solution results
rownames	Row names
rowmass	Row weights
rowdist	Row logratio distances to centroid
rowinertia	Row inertias
rowcoord	Row standard coordinates
rowpcoord	Row principal coordinates
rowsup	Indices of row supplementary points
colnames	Column names
colmass	Column weights
coldist	Column logratio distances to centroid
colinertia	Column inertias
colcoord	Column standard coordinates
colpcoord	Column principal coordinates
N	The compositional data table

**Author(s)**

Michael Greenacre

**References**

Aitchison, J. and Greenacre, M. (2002), Biplots of compositional data, *Applied Statistics* 51, 375-392.

Greenacre, M. and Lewi, P.J. (2009), Distributional equivalence and subcompositional coherence in the analysis of compositional data, contingency tables and ratio scale measurements. *Journal of Classification* 26, 29-54.

Greenacre, M. (2020), Amalgamations are valid in compositional data analysis, can be used in agglomerative clustering, and their logratios have an inverse transformation. *Applied Computing and Geosciences* 5, 100017.

**See Also**

[plot.ca](#), [summary.ca](#), [print.ca](#)

**Examples**

```
# (weighted) LRA of the RomanCups data set, showing default symmetric map
data("cups")
PLOT.LRA(LRA(cups))
# (unweighted) LRA of the RomanCups data set, showing default symmetric map
# the solution is completely different
PLOT.LRA(LRA(cups, weight=FALSE))
```

---

 PCA *Principal component analysis*


---

**Description**

Computation of weighted or unweighted principal component analysis of a matrix of interval-scale data (e.g. a matrix of logratios).

**Usage**

```
PCA(data, nd = 2, weight = TRUE, row.wt = NA, suprow = NA)
```

**Arguments**

data	A data frame or matrix of interval-scale data, or logratio object from functions ALR, CLR or LR
nd	Number of dimensions for summary solution if not 2 (default)
weight	TRUE (default) for column weighting, FALSE for unweighted analysis, or a vector of user-defined column weights
row.wt	Optional user-defined set of positive weights for the rows (samples) (default: equal weights)
suprow	Indices of rows that are supplementary points (NOTE: this option is not implemented in this version)

**Details**

The function PCA computes an unstandardized principal component analysis, based on the singular value decomposition, of a matrix of interval-scale data, usually a matrix of logratios in the context of this package (but it can be used for general data as well). For general usage the unweighted option `weight = FALSE` might be preferred, but the default is weighted in the present context of compositional data.

User-specified weights can be supplied, for the rows and/or the columns. Usually row weights are not specified, and are equal unless intentional weighting of the samples is desired. User-specified part weights can be provided using the `weight` option.

Supplementary rows and columns can be declared (also known as passive points) – these do not contribute to the solution but are positioned on the solution axes. Notice that this option is not implemented in the present version, but will appear in the next one.

The function borrows the structure and functions of the `ca` package, which is required, and produces a `ca` object, and the same `print`, `summary` and `plot` methods can be used, as for a `ca` object.

**Value**

sv	Singular values
nd	Dimension of the solution
rownames	Row names

rowmass	Row weights
rowdist	Row logratio distances to centroid
rowinertia	Row variances
rowcoord	Row standard coordinates
rowpcoord	Row principal coordinates
rowsup	Indices of row supplementary points
colnames	Column names
colmass	Column weights
coldist	Column logratio distances to centroid
colinertia	Column variances
colcoord	Column standard coordinates
colpcoord	Column principal coordinates
N	The data table

### Author(s)

Michael Greenacre

### References

Aitchison, J. and Greenacre, M. (2002), Biplots of compositional data, *Applied Statistics* 51, 375-392.

Greenacre, M. (2010), *Biplots in Practice*, BBVA Foundation, Bilbao. Free download from [www.multivariatestatistics.org](http://www.multivariatestatistics.org)

### See Also

PLOT.PCA, [plot.ca](#), [summary.ca](#), [print.ca](#)

### Examples

```
# compute logratios of Vegetables data set
data("veg")
veg.LR <- LR(veg)
# unweighted PCA biplot of the results
veg.pca <- PCA(veg.LR$LR, weight=FALSE)
PLOT.PCA(veg.pca, map="asymmetric")
```

---

PLOT.CA

*Plot the results of a correspondence analysis*


---

### Description

Various maps and biplots of the results of a correspondence analysis using function CA.

### Usage

```
PLOT.CA(obj, map="symmetric", rescale=1, dim=c(1,2), axes.inv = c(1,1), main="",
        cols=c("blue","red"), colarrows = "pink", cexs=c(0.8,0.8), fonts=c(2,4))
```

### Arguments

obj	A CA object created using function CA
map	Choice of scaling of rows and columns: "symmetric" (default), "asymmetric" or "contribution"
rescale	A rescaling factor applied to column coordinates (default is 1 for no rescaling)
dim	Dimensions selected for horizontal and vertical axes of the plot (default is c(1,2))
main	Title for plot
axes.inv	Option for reversing directions of horizontal and vertical axes (default is c(1,1) for no reversing, change one or both to -1 for reversing)
cols	Colours for row and column labels (default is c("blue","red"))
colarrows	Colour for arrows in asymmetric and contribution biplots (default is "pink")
cexs	Character expansion factors for row and column labels (default is c(0.8,0.8))
fonts	Fonts for row and column labels (default is c(2,4))

### Details

The function PLOT.CA makes a scatterplot of the results of a correspondence analysis (computed using function CA), with various options for scaling the results and changing the direction of the axes. By default, dimensions 1 and 2 are plotted on the horizontal and vertical axes, and it is assumed that row points refer to samples and columns to variables.

By default, the symmetric scaling is used, where both rows and columns are in principal coordinates and have the same amount of weighted variance (i.e. inertia) along the two dimensions. The other options are biplots: the asymmetric option, when columns are in standard coordinates, and the contribution option, when columns are in contribution coordinates. In cases where the row and column displays occupy widely different extents, the column coordinates can be rescaled using the rescale option.

### Author(s)

Michael Greenacre

**References**

Greenacre, M. (2013), Contribution biplots, Journal of Computational and Graphical Statistics, 22, 107-122.

**See Also**

[CA, plot.ca](#)

**Examples**

```
data("cups")
cups.ca <- CA(cups)
PLOT.CA(cups.ca, map="contribution", rescale=0.2)
# Compare the above plot with that of a weighted LRA -- practically the same
cups.lra <- LRA(cups)
PLOT.LRA(cups.lra, map="contribution", rescale=0.2)
```

---

PLOT.LRA

---

*Plot the results of a logratio analysis*


---

**Description**

Various maps and biplots of the results of a logratio analysis using function LRA.

**Usage**

```
PLOT.LRA(obj, map="symmetric", rescale=1, dim=c(1,2), axes.inv = c(1,1), main="",
  cols=c("blue","red"), colarrows = "pink", cexs=c(0.8,0.8), fonts=c(2,4))
```

**Arguments**

obj	An LRA object created using function LRA
map	Choice of scaling of rows and columns: "symmetric" (default), "asymmetric" or "contribution"
rescale	A rescaling factor applied to column coordinates (default is 1 for no rescaling)
dim	Dimensions selected for horizontal and vertical axes of the plot (default is c(1,2))
axes.inv	Option for reversing directions of horizontal and vertical axes (default is c(1,1) for no reversing, change one or both to -1 for reversing)
main	Title for plot
cols	Colours for row and column labels (default is c("blue","red"))
colarrows	Colour for arrows in asymmetric and contribution biplots (default is "pink")
cexs	Character expansion factors for row and column labels (default is c(0.8,0.8))
fonts	Fonts for row and column labels (default is c(2,4))

## Details

The function `PLOT.LRA` makes a scatterplot of the results of a logratio analysis (computed using function `LRA`), with various options for scaling the results and changing the direction of the axes. By default, dimensions 1 and 2 are plotted on the horizontal and vertical axes, and it is assumed that row points refer to samples and columns to compositional parts.

By default, the symmetric scaling is used, where both rows and columns are in principal coordinates and have the same amount of weighted variance along the two dimensions. The other options are the asymmetric option, when columns are in standard coordinates, and the contribution option, when columns are in contribution coordinates. In cases where the row and column displays occupy widely different extents, the column coordinates can be rescaled using the `rescale` option.

## Author(s)

Michael Greenacre

## References

Greenacre, M. (2013), Contribution biplots, *Journal of Computational and Graphical Statistics*, 22, 107-122.

## See Also

[plot.ca](#)

## Examples

```
# perform LRA on the vegetable compositions (unweighted form)
data("veg")
veg.lra <- LRA(veg, weight=FALSE)
PLOT.LRA(veg.lra)
# perform LRA on the Roman cups data set and plot the results (weighted form)
data("cups")
cups.lra <- LRA(cups)
PLOT.LRA(cups.lra, map="contribution", rescale=0.2)
```

---

PLOT.PCA

*Plot the results of a principal component analysis*

---

## Description

Various maps and biplots of the results of a principal component analysis using function `PCA`.

## Usage

```
PLOT.PCA(obj, map="symmetric", rescale=1, dim=c(1,2), axes.inv = c(1,1),
          main="", cols=c("blue","red"), colarrows = "pink", cex=c(0.8,0.8),
          fonts=c(2,4))
```

**Arguments**

obj	An LRA object created using function LRA
map	Choice of scaling of rows and columns: "symmetric" (default), "asymmetric" or "contribution"
rescale	A rescaling factor applied to column coordinates (default is 1 for no rescaling)
dim	Dimensions selected for horizontal and vertical axes of the plot (default is c(1,2))
axes.inv	Option for reversing directions of horizontal and vertical axes (default is c(1,1) for no reversing, change one or both to -1 for reversing)
main	Title for plot
cols	Colours for row and column labels (default is c("blue","red"))
colarrows	Colour for arrows in asymmetric and contribution biplots (default is "pink")
cexs	Character expansion factors for row and column labels (default is c(0.8,0.8))
fonts	Fonts for row and column labels (default is c(2,4))

**Details**

The function PLOT.PCA makes a scatterplot of the results of a logratio analysis (computed using function PCA), with various options for scaling the results and changing the direction of the axes. By default, dimensions 1 and 2 are plotted on the horizontal and vertical axes, and it is assumed that row points refer to samples and columns to variables.

By default, the symmetric scaling is used, where both rows and columns are in principal coordinates and have the same amount of weighted variance along the two dimensions. The other options are biplots: the asymmetric option, when columns are in standard coordinates, and the contribution option, when columns are in contribution coordinates. In cases where the row and column displays occupy widely different extents, the column coordinates can be rescaled using the rescale option.

**Author(s)**

Michael Greenacre

**References**

Greenacre, M. (2013), Contribution biplots, Journal of Computational and Graphical Statistics, 22, 107-122.

**See Also**

[plot.ca](#)

**Examples**

```
# perform weighted PCA on the ALRs of the Roman cups data set
# where the first oxide silica is chosen as the denominator
data("cups")
cups.alr <- ALR(cups, denom=1)
cups.pca <- PCA(cups.alr)
PLOT.PCA(cups.pca, map="contribution", rescale=0.2, axes.inv=c(1,-1))
```



---

PLOT.RDA

*Plot the results of a redundancy analysis*


---

**Description**

Various maps and biplots/triplets of the results of a redundancy analysis using function RDA.

**Usage**

```
PLOT.RDA(obj, map="symmetric", indcat=NA, rescale=1, dim=c(1,2), axes.inv=c(1,1),
  main="", rowstyle=1, cols=c("blue","red","forestgreen"),
  colarrows=c("pink","lightgreen"), colrows=NA, pchrows=NA, colcats=NA,
  cexs=c(0.8,0.8,0.8), fonts=c(2,4,4))
```

**Arguments**

obj	An RDA object created using function RDA
map	Choice of scaling of rows and columns: "symmetric" (default), "asymmetric" or "contribution"
indcat	A vector indicating which of the covariates are dummy (or fuzzy) variables
rescale	A rescaling factor applied to column coordinates (default is 1 for no rescaling). If rescale is a vector with two values, the first applies to the column coordinates and the second to the covariate coordinates.
dim	Dimensions selected for horizontal and vertical axes of the plot (default is c(1,2))
axes.inv	Option for reversing directions of horizontal and vertical axes (default is c(1,1) for no reversing, change one or both to -1 for reversing)
main	Title for plot
rowstyle	Scaling option for row coordinates, either 1 (SVD coordinates, default) or 2 (as supplementary points)
cols	Colours for row and column and covariate labels (default is c("blue","red","forestgreen"))
colarrows	Colour for arrows in asymmetric or contribution biplots, for columns and covariates (default is c("pink","lightgreen"))
colrows	Optional vector of colours for rows
pchrows	Optional vector of point symbols for rows
colcats	Optional vector of colours for covariate categories (dummy variables)
cexs	Vector of character expansion factors for row and column and covariate labels (default is c(0.8,0.8,0.8))
fonts	Vector of font styles for row and column and covariate labels (default is c(2,4,4))

**Details**

The function `PLOT.RDA` makes a scatterplot of the results of a redundancy analysis (computed using function `RDA`), with various options for scaling the results and changing the direction of the axes. By default, dimensions 1 and 2 are plotted on the horizontal and vertical axes, and it is assumed that row points refer to samples and columns to compositional parts. Covariates are plotted according to their regression coefficients with the RDA dimensions, and if they contain dummy (or fuzzy) variables these are indicated by the option `indcat`, and hence plotted as centroids not arrows.

By default, the symmetric scaling is used, where both rows and columns are in principal coordinates and have the same amount of weighted variance along the two dimensions. The other options are the asymmetric option, when columns are in standard coordinates, and the contribution option, when columns are in contribution coordinates. In cases where the row and column displays as well as the covariate positions occupy widely different extents, the column and covariate coordinates can be rescaled using the `rescale` option.

**Author(s)**

Michael Greenacre

**See Also**

[RDA](#)

**Examples**

```
# see the use of PLOT.RDA in the example of the RDA function
```

---

PLR

*Pivot logratios*

---

**Description**

Computation of the set of pivot logratios(PLRs) based on the specified ordering of parts

**Usage**

```
PLR(data, ordering=1:ncol(data), weight=TRUE)
```

**Arguments**

<code>data</code>	A compositional data frame or matrix
<code>ordering</code>	The ordering of the parts to be used in the PLRs (by default, the original ordering of the columns)
<code>weight</code>	Logical indicating if varying weights are returned (default:TRUE). If FALSE, weights based on equally-weighted parts are returned. Alternatively a set of positive weights can be specified.

**Details**

The function PLR computes the set of pivot logratios according to the ordering of the parts.

**Value**

LR                    The pivot logratios (PLRs)  
 LR.wt                The weights assigned to the PLRs

**Author(s)**

Michael Greenacre

**References**

Hron K., Filzmoser P., de Caritat P., Fiserova E., Gardlo A. (2017). Weighted pivot coordinates for copositional data and their application to geochemical mapping. *Mathematical Geosciences* 49, 777-796.

**See Also**

[ILR](#), [SLR](#), [CLR](#), [ALR](#), [LR](#)

**Examples**

```
data(veg)
PLR(veg, ordering=c(1,3,2))
```

---

 RDA

*Redundancy analysis*


---

**Description**

Computation of weighted or unweighted redundancy analysis of a samples-by-parts compositional data table, given a set of covariates.

**Usage**

```
RDA(data, cov=NA, nd = NA, weight = TRUE, suprow = NA, row.wt = NA)
```

**Arguments**

data                A data frame or matrix of interval-scale data, e.g. logratios (which are preferably in a list object with weights)  
 cov                List of covariates for constraining solution  
 nd                 Number of dimensions for summary output, by default the number of constraining dimensions

weight	TRUE (default) when weights are in data list object, FALSE for unweighted analysis, or a vector of user-defined part weights
suprow	Indices of rows that are supplementary (passive) points (NOTE: this option is not implemented in this version)
row.wt	Optional user-defined set of positive weights for the rows (samples) (default: equal weights)

### Details

The function RDA computes a redundancy analysis of a matrix of interval-scaled data, constrained by a matrix of covariates, using the singular value decomposition. By default weights are assumed in the data list object. For the unweighted logratio analysis, specify the option `weight=FALSE`. If `weight = TRUE` (the default) it is assumed that the weights are included in the data object, which comes from one of the logratio functions. User-specified part weights can be provided using the same `weight` option.

Usually row weights are not specified, they are equal unless intentional weighting of the samples is desired. Supplementary rows can be declared (also known as passive points) – these do not contribute to the solution but are positioned on the solution axes. This option will be available in the next release of the package.

### Value

sv	Singular values
nd	Number of dimensions in the solution output
rownames	Row names
rowmass	Row weights
rowdist	Row distances to centroid
rowinertia	Row variances
rowcoord	Row standard coordinates
rowpcoord	Row principal coordinates
rowsup	Indices of row supplementary points
colnames	Column names
colmass	Column weights
coldist	Column logratio distances to centroid
colinertia	Column variances
colcoord	Column standard coordinates
colpcoord	Column principal coordinates
covcoord	Regression coordinates of constraining variables
covnames	Names of constraining variables
N	The data table (usually logratios in this package)
cov	The table of covariates

**Author(s)**

Michael Greenacre

**References**

Van den Wollenbergh, A. (1977), Redundancy analysis. An alternative to canonical correlation analysis, *Psychometrika* 42, 207-219.  
 Greenacre, M. (2013), Contribution biplots, *Journal of Computational and Graphical Statistics* 22, 107-122.

**See Also**

[PLOT.RDA](#), [CLR](#), [LR](#), [DUMMY](#)

**Examples**

```
# Data frame fish has sex, habitat and mass in first columns,
# then morphometric data in remaining columns
data("fish")
sex    <- fish[,1]
habitat <- fish[,2]
mass   <- fish[,3]
fishm  <- as.matrix(fish[,4:29])
# Convert to compositional data matrix
fishm  <- CLOSE(fishm)
# Compute logarithm of mass and interaction of sex (F/M) and habitat (L/P) categories
logmass <- log(mass)
sexhab  <- 2*(sex-1)+habitat
sexhab.names <- c("FL", "FP", "ML", "MP")
rownames(fishm) <- sexhab.names[sexhab]
# Create dummy variables for sexhab and create matrix of covariates
sexhab.Z <- DUMMY(sexhab, catnames=sexhab.names)
vars     <- cbind(logmass, sexhab.Z)
# Perform RDA on centred logratios
require(ca)
fish.rda <- RDA(CLR(fishm), cov=vars)
# Plot results
# (for more options see Appendix of Compositional Data Analysis in Practice)
PLOT.RDA(fish.rda, map="contribution", rescale=0.05, indcat=2:5,
         colrows=rainbow(4, start=0.1, end=0.8)[sexhab], cexs=c(0.8,0.8,1))
```

---

 SLR

---

*Amalgamation (summed) logratio*


---

**Description**

Computation of a single amalgamation (summed) logratio

**Usage**

```
SLR(data, numer=NA, denom=NA, weight=TRUE)
```

**Arguments**

data	A compositional data frame or matrix
numer	Vector of parts in the numerator
denom	Vector of parts in the denominator
weight	Logical indicating if a varying weight is returned (default:TRUE). If FALSE, a weight based on equally-weighted parts is returned. Alternatively a positive weight can be specified.

**Details**

The function SLR computes a single amalgamation logratio based on the specified numerator and denominator parts that define the two summations in the ratio.

**Value**

LR	The amalgamation (summed) logratio (SLR)
LR.wt	The weight assigned to the SLR

**Author(s)**

Michael Greenacre

**References**

Aitchison, J. (1986), *The Statistical Analysis of Compositional Data*, Chapman & Hall.  
Greenacre, M. (2018), *Compositional Data Analysis in Practice*, Chapman & Hall / CRC Press.

**See Also**

[ILR](#), [ALR](#), [CLR](#), [PLR](#), [LR](#)

**Examples**

```
data(veg)  
SLR(veg, numer=1, denom=2:3)
```

---

STEP *Stepwise selection of logratios*

---

**Description**

Stepwise selection of pairwise logratios that explain maximum variance in a target matrix.

**Usage**

```
STEP(data, datatarget=data, previous=NA, previous.wt=NA, weight=TRUE,
      random=FALSE, nsteps=min(ncol(data), ncol(datatarget))-1, top=1)
```

**Arguments**

data	A data frame or matrix of compositional data on which pairwise logratios are computed
datatarget	A matrix of interval-scale data, with as many rows as data, which serves as the target matrix whose variance is to be explained (by default it is the same matrix as data, in which case total logratio variance is to be explained)
previous	A vector or matrix of variables to be forced in before logratios are sought
previous.wt	Possible weights of the variable(s) forced in before logratios are sought (if not specified, weights of 1 are assumed)
weight	TRUE (default) when weights are in data list object, FALSE for unweighted analysis, or a vector of user-defined part weights
random	TRUE if a random selection is made of tied logratios; FALSE (default) if logratio that maximizes Procrustes correlation is chosen
nsteps	Number of steps to take (by default, one less than the number of columns of data and of datatarget, whichever is smaller)
top	Number of top variance-explaining logratios returned after last step (by default, 1, i.e. the best)

**Details**

The function STEP sequentially computes the logratios in a data matrix (usually compositional) that best explain the variance in a second matrix, called the target matrix. By default, the target matrix is the same matrix, in which case the logratios that best explain the logratio variance in the same matrix are computed. In this case, weights for the data matrix are assumed by default, proportional to part means of the compositional data matrix. For the unweighted logratio variance, specify the option `weight=FALSE`. User-specified weights on the columns of the data matrix (usually compositional parts) can be provided using the same `weight` option.

If the target matrix is a different matrix, it is the logratio variance of that matrix that is to be explained. An option for the target matrix to be any response matrix will be in the next release.

If `nsteps > 1` and `top=1` the results are in the form of an optimal set of logratios that sequentially add maximum explained variance at each step. If `top>1` then at the last step the ordered list of

top variance-explaining logratios is returned, which allows users to make an alternative choice of the logratio based on substantive knowledge. Hence, if `nsteps=1` and `top=10`, for example, the procedure will move only one step, but list the top 10 logratios for that step. If `top=1` then all results with extension `.top` related to the top ratios are omitted because they are already given.

### Value

<code>names</code>	Names of maximizing ratios in stepwise process
<code>ratios</code>	Indices of ratios
<code>logratios</code>	Matrix of logratios
<code>R2max</code>	Sequence of maximum cumulative explained variances
<code>pro.cor</code>	Corresponding sequence of Procrustes correlations
<code>names.top</code>	Names of "top" ratios at last step
<code>ratios.top</code>	Indices of "top" ratios
<code>logratios.top</code>	Matrix of "top" logratios
<code>R2.top</code>	Sequence of "top" cumulative explained variances (in descending order)
<code>pro.cor.top</code>	Corresponding sequence of "top" Procrustes correlations
<code>totvar</code>	Total logratio variance of target matrix

### Author(s)

Michael Greenacre

### References

- Van den Wollenbergh, A. (1977), Redundancy analysis. An alternative to canonical correlation analysis, *Psychometrika* 42, 207-219.
- Greenacre, M. (2018), Variable selection in compositional data analysis using pairwise logratios, *Mathematical Geosciences*, DOI: 10.1007/s11004-018-9754-x.
- Greenacre, M. (2018), *Compositional Data Analysis in Practice*, Chapman & Hall / CRC

### See Also

[PLOT.RDA](#), [CLR](#), [LR](#), [ALR](#)

### Examples

```
# Stepwise selection of ratios for RomanCups data set
data(cups)
# Set seed to obtain same results as in Appendix C of Greenacre (2018)
set.seed(2872)
STEP(cups, random=TRUE)
# Select best ratio, but output "top 5"
STEP(cups, nsteps=1, top=5)
```



---

STEPR	<i>Stepwise selection of pairwise logratios for generalized linear modelling</i>
-------	--

---

**Description**

Three different algorithms for selecting pairwise logratios that best explain/predict a response variable, which could be continuous, binary or count

**Usage**

```
STEPR(data, y, method = NA, family = "gaussian", nsteps = ncol(data)-1,
      top = 1, previous = NA, criterion = "Bonferroni", alpha = 0.05,
      previousparts=NA, denom=NA)
```

**Arguments**

data	A data frame or matrix of compositional data on which the pairwise logratios will be constructed and selected
y	The response variable: a numeric variable for regression (default), a binary factor for logistic regression or a numeric count for Poisson regression
method	The selection method: 1 (unrestricted selection of logratios), 2 (restricted to non-overlapping parts), 3 (additive logratios)
family	The distribution used in the generalized linear model family: "gaussian" (default, for multiple regression), "binomial" (for logistic regression of binary response), or "poisson" (for Poisson regression)
nsteps	The maximum number of steps taken, by default one less than the number of parts
top	When one step is taken (nsteps=1), the ordered list of top logratios with the highest improvements in the likelihood function, for selection based on domain knowledge
previous	For specifying variable(s) to be included before stepwise selection takes place; these can be non-compositional variables and/or specific pairwise logratios computed in previous runs of STEPR or by hand; the matrix (or vector for a single variable) of values must be supplied
criterion	Criterion for stopping the stepwise selection: "Bonferroni" (default), "AIC", "BIC", or NA for no stopping until maximum specified or permissible logratios entered
alpha	Overall significance level (default is 0.05)
previousparts	(For method 2) The sequence numbers of the logratios, if any, forced in using the previous option
denom	(For method 3) The sequence number of the part used in denominator; for use when additive logratios are forced in using previous option or to select a set of additive logratios with specific reference from the start

### Details

The function STEP<sub>R</sub> performs stepwise selection of pairwise logratios with the objective of explaining/predicting a response variable, in the framework of generalized linear modelling where the response can be numeric continuous (regression analysis), or a binary factor (logistic regression), or a numeric count (Poisson regression). The corresponding family option has to be indicated if the regression is logistic or Poisson. The different method options for the stepwise selection are method = 1 (unrestricted selection of logratios, any logratios can be selected irrespective of the previous ones), method = 2 (restricted to non-overlapping parts, each part participates at most in one logratio, so that parts in previously selected logratios are excluded in subsequent steps; logratio effects can be interpreted as under orthogonality), method = 3 (additive logratios, only logratios with the same denominator as the first selected logratio are considered; the result is an additive logratio transformation on a subcomposition) Three alternative stopping criteria can be specified, otherwise the procedure executes as many steps as the value of nsteps. These are (in increasing strictness), "AIC", "BIC" and "Bonferroni" (the default).

### Value

rationames	Names of the selected logratios
ratios	The sequence numbers of the selected parts in each ratio
logratios	Matrix of selected logratios
logLik	The $-2 \times \log$ -likelihood sequence for the steps
deviance	The deviance sequence for the steps
AIC	The AIC sequence for the steps
BIC	The BIC sequence for the steps
Bonferroni	The Bonferroni sequence for the steps
null.deviance	The null deviance for the regression

(Notice that for logLik, AIC, BIC and Bonferroni, the values for one more step are given, so that the stopping point can be confirmed.)

And the following if top > 1:

ratios.top	The top ratios and the sequence numbers of their parts
logratios.top	The matrix of top logratios
logLik.top	The set of top $-2 \times \log$ -likelihoods
deviance.top	The set of top deviances
AIC.top	The set of top AICs
BIC.top	The set of top BICs
Bonferroni.top	The set of top Bonferronis

### Author(s)

Michael Greenacre

## References

- Coenders, G. and Greenacre, M. (2021), Three approaches to supervised learning for compositional data with pairwise logratios. aRxiv preprint. URL:<https://arxiv.org/abs/2111.08953>
- Coenders, G. and Pawlowsky-Glahn, V. (2020), On interpretations of tests and effect sizes in regression models with a compositional predictor. SORT, 44:201-220
- Greenacre, M. (2021), Compositional data analysis, Annual Review of Statistics and its Application, 8: 271-299

## See Also

[ALR](#), [STEP](#), [glm](#)

## Examples

```
# For the fish morphometric data, first close (normalize, although not necessary)
# then loop over the 26*25/2 = 325 possible logratios stepwise
data(fish)
habitat <- fish[,2]
morph <- CLOSE(fish[,4:29])
# predict habitat binary classification from morphometric ratios
fish.step1 <- STEPR(morph, as.factor(habitat), method=1, family="binomial")
# [1] "Criterion increases when 3-th ratio enters"
fish.step1$names
# [1] "Bac/Hg" "Hw/J1"
# perform logistic regression with selected logratios
fish.glm <- glm(as.factor(habitat) ~ fish.step1$logratios, family="binomial")
summary(fish.glm)
fish.pred1 <- predict(fish.glm)
table(fish.pred1>0.5, habitat)
#   habitat
#     1  2
# FALSE 56 11
# TRUE   3  5
# (Thus 61/75 correct predictions)
#
# force the sex variable in at the first step before selecting logratios
# and using more strict Bonferroni default
sex <- as.factor(fish[,1])
fish.step2 <- STEPR(morph, as.factor(habitat), method=1, previous=sex, family="binomial")
# [1] "Criterion increases when 3-th ratio enters"
fish.step2$names
# [1] "Bac/Hg" "Hw/J1"
# perform logistic regression with sex and selected logratios
fish.glm <- glm(as.factor(habitat) ~ sex + fish.step2$logratios, family="binomial")
summary(fish.glm)
# (sex not significant)
#
# check the top 10 ratios at Step 1 to allow domain knowledge to operate
fish.step3 <- STEPR(morph, as.factor(habitat), method=1, nsteps=1, top=10, family="binomial")
cbind(fish.step3$ratios.top, fish.step3$BIC.top)
#   row col
```

```

# Bac/Hg  8  19 67.93744
# Bp/Hg   7  19 69.87134
# Jl/Hg   6  19 70.31554
# Jw/Bp   5   7 71.53671
# Jw/Jl   5   6 71.57122
# Jw/Bac  5   8 71.69294
# Fc/Hg  10  19 72.38560
# Hw/Bac  1   8 73.25325
# Jw/Fc   5  10 73.48882
# Hw/Bp   1   7 73.55621
# Suppose 5th in list, Jw/Jl (Jaw width/Jaw length), preferred at the first step
fish.step4 <- STEPR(morph, as.factor(habitat), method=1,
                    previous=fish.step3$logratios.top[,5], family="binomial")
# [1] "Criterion increases when 2-th ratio enters"
fish.step4$names
# [1] "Bac/Hg"
# So after Jw/Jl forced in only Bac/Hg enters, the best one originally

```

---

time

*Dataset: TimeBudget*


---

## Description

This data set consists of the average percentage breakdown of time use into six categories, for 16 countries, split by males and females.

## Usage

```
data(time)
```

## Format

Data matrix containing the 32 x 6 matrix. Row samples are labelled by the two-character country code and m (male) or f (female).

## Source

Greenacre M., *Compositional Data Analysis in Practice*, Chapman & Hall / CRC, 2018.

---

**VAR***Variance of a vector of observations, dividing by n rather than n-1*

---

**Description**

This function computes the usual variance but divides by n, not by n-1.

**Usage**

```
VAR(x)
```

**Arguments**

x                      Vector of values for which variance is computed

**Details**

To think of each of n observations weighted by 1/n this function VAR computes squared deviations from the mean and averages them. Thus, the sum of squared deviations is divided by n rather than by n-1, as for the unbiased estimate of the variance.

**Value**

The value of the variance.

**Author(s)**

Michael Greenacre

**References**

Greenacre, M. (2018), *Compositional Data Analysis in Practice*, Chapman & Hall / CRC.

**See Also**

[LR.VAR](#), [CLOSE](#)

**Examples**

```
data(cups)
cups <- CLOSE(cups)

# variances using base R function var
apply(cups, 2, var)

# variances using easyCODA function VAR
apply(cups, 2, VAR)
```

---

veg *Dataset: Vegetables*

---

### Description

This data set consists of the protein, carbohydrate and fat compositions of 10 different vegetables. Compositions are expressed as percentages.

### Usage

```
data(veg)
```

### Format

Data frame containing the 10 x 3 matrix.

### Source

US Department of Agriculture, <https://ndb.nal.usda.gov/ndb/nutrients/index>

---

WARD *Ward clustering of a compositional data matrix*

---

### Description

This function clusters the rows (or the columns, if the matrix is transformed) of a compositional data matrix, using weighted Ward clustering of the logratios.

### Usage

```
WARD(LRdata, weight=TRUE, row.wt=NA)
```

### Arguments

LRdata	Matrix of logratios, either a vector or preferably the logratio object resulting from one of the functions ALR, CLR, PLR or LR (usually CLRs will be used)
weight	TRUE (default) for weighted analysis (in which case weights are in the logratio object), FALSE for unweighted analysis, or a vector of user-defined column weights
row.wt	Optional set of row weights (default is equal weights when row.wt=NA)

**Details**

The function `WARD` performs a weighted WARD hierarchical clustering on the rows of an input set of logratios, usually CLR-transformed. (This would be equivalent to performing the clustering on all pairwise logratios). If the columns of the logratio matrix are unweighted, specify the option `weight=FALSE`: they will then get equal weights. The default `weight=TRUE` option implies that column weights are provided, either in the input list object `LRdata`, as `LRdata$LR.wt`, or as a vector of user-specified weights using the same `weight` option.

**Value**

An object which describes the tree produced by the clustering process on the `n` objects. The object is a list with components:

<code>merge</code>	an <code>n-1</code> by 2 matrix. Row <code>i</code> of <code>merge</code> describes the merging of clusters at step <code>i</code> of the clustering. If an element <code>j</code> in the row is negative, then observation <code>-j</code> was merged at this stage. If <code>j</code> is positive then the merge was with the cluster formed at the (earlier) stage <code>j</code> of the algorithm. Thus negative entries in <code>merge</code> indicate agglomerations of singletons, and positive entries indicate agglomerations of non-singletons.
<code>height</code>	a set of <code>n-1</code> real values (non-decreasing for ultrametric trees). The clustering height: that is, the value of the criterion associated with the clustering method for the particular agglomeration.
<code>order</code>	a vector giving the permutation of the original observations suitable for plotting, in the sense that a cluster plot using this ordering and matrix <code>merge</code> will not have crossings of the branches

**Author(s)**

Michael Greenacre

**References**

Greenacre, M. (2018), *Compositional Data Analysis in Practice*, Chapman & Hall / CRC.

**See Also**

[hclust](#), [CLR](#), [LR.VAR](#), [CLOSE](#)

**Examples**

```
# clustering steps for unweighted and weighted logratios
# for both row- and column-clustering
data(cups)
cups <- CLOSE(cups)

# unweighted logratios: clustering samples
cups.uclr <- CLR(cups, weight=FALSE)
cups.uward <- WARD(cups.uclr, weight=FALSE) # weight=FALSE not needed here,
# as equal weights are in object
```

```
plot(cups.ward)
# add up the heights of the nodes
sum(cups.ward$height)
# [1] 0.02100676
# check against the total logratio variance
LR.VAR(cups.uclr, weight=FALSE)
# [1] 0.02100676

# unweighted logratios: clustering parts
tcups <- t(cups)
tcups.uclr <- CLR(tcups, weight=FALSE)
tcups.ward <- WARD(tcups.uclr, weight=FALSE) # weight=FALSE not needed here,
# as equal weights are in object

plot(tcups.ward, labels=colnames(cups))
sum(tcups.ward$height)
# [1] 0.02100676
LR.VAR(tcups.uclr, weight=FALSE)
# [1] 0.02100676

# weighted logratios: clustering samples
cups.clr <- CLR(cups)
cups.ward <- WARD(cups.clr)
plot(cups.ward)
sum(cups.ward$height)
# [1] 0.002339335
LR.VAR(cups.clr)
# [1] 0.002339335

# weighted logratios: clustering parts
# weight=FALSE is needed here, since we want equal weights
# for the samples (columns of tcups)
tcups.clr <- CLR(tcups, weight=FALSE)
tcups.ward <- WARD(tcups.clr, row.wt=colMeans(cups))
plot(tcups.ward, labels=colnames(cups))
  sum(tcups.ward$height)
# [1] 0.002339335
LR.VAR(tcups.clr, row.wt=colMeans(cups))
# [1] 0.002339335
```



# Index

- \* **coding**
  - DUMMY, 16
- \* **datasets**
  - cups, 14
  - fish, 18
  - time, 44
  - veg, 46
- \* **logratio**
  - ALR, 6
  - CLR, 13
  - ILR, 18
  - invALR, 19
  - invCLR, 20
  - invSLR, 21
  - LR, 22
  - LR.VAR, 23
  - PLR, 34
  - SLR, 37
- \* **multivariate**
  - ACLUST, 4
  - CA, 9
  - FINDALR, 16
  - LRA, 25
  - PCA, 27
  - PLOT.CA, 29
  - PLOT.LRA, 30
  - PLOT.PCA, 31
  - PLOT.RDA, 33
  - RDA, 35
  - STEP, 39
  - STEPR, 41
  - WARD, 46
- \* **package**
  - easyCODA-package, 2
- \* **variance**
  - VAR, 45
- \* **visualization**
  - BAR, 7
  - CIplot\_biv, 10
  - DOT, 14
- ACLUST, 4
- ALR, 6, 13, 17, 19–24, 35, 38, 40, 43
- BAR, 7, 15
- CA, 9, 30
- ca, 4
- CIplot\_biv, 10
- CLOSE, 6, 12, 45, 47
- CLR, 6, 7, 13, 20–24, 35, 37, 38, 40, 47
- cups, 14
- DOT, 8, 11, 14
- DUMMY, 16, 37
- easyCODA-package, 2
- FINDALR, 16
- fish, 18
- glm, 43
- hclust, 6, 47
- ILR, 18, 35, 38
- invALR, 7, 13, 19, 21–24
- invCLR, 7, 13, 20, 20, 23, 24
- invSLR, 21
- LR, 7, 13, 19, 20, 22, 24, 35, 37, 38, 40
- LR.VAR, 6, 7, 13, 20–23, 23, 45, 47
- LRA, 25
- PCA, 27
- PLOT.CA, 10, 29
- plot.ca, 10, 26, 28, 30–32
- PLOT.LRA, 30
- PLOT.PCA, 31
- PLOT.RDA, 33, 37, 40
- PLR, 19, 34, 38

`print.ca`, [10](#), [26](#), [28](#)

RDA, [34](#), [35](#)

SLR, [19](#), [35](#), [37](#)

STEP, [39](#), [43](#)

STEPR, [41](#)

`summary.ca`, [10](#), [26](#), [28](#)

time, [44](#)

VAR, [45](#)

veg, [46](#)

WARD, [6](#), [46](#)